

Summary of *Beam Polarization in Future Colliders* Mini-Workshop

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**Conference at IAS Program of High Energy Physics,
Hong Kong University of Science and Technology
January 7-25, 2019**

About Mini-Workshop

- **General topic**
 - “Polarized Beams: A Brief History and Future Prospect” by Yaroslav Derbenev (JLab)
- **Machine Overview**
 - “Introduction to CEPC “ by Jie Gao (IHEP)
- **e+e- colliders at low to medium energy**
 - “BINP's Polarization Proposal for Tau-Charm Factory” by Ivan Koop (BINP)
- **e+e- collider at energy frontier**
 - “Resonant Depolarization at Z and W Beam Energy” by Ivan Koop (BINP)
 - “Polarized Electron and Positron Beams in CEPC” by Zhe Duan (IHEP)
 - “Preliminary Studies of Beam Polarization in CEPC” by Wenhao Xia (IHEP)
- **e-p and e-A colliders**
 - “Beam Polarization in Future Colliders (eRHIC and FCC-ee)” by Eliana Gianfelice-Wendt (FNAL)
 - “JLEIC Electron Beam Polarization” by Yuhong Zhang (JLab)
 - “Spin Matching in Electron (Positron) Rings” by Vadim Ptitsyn (BNL)
- **Electron/positron sources**
 - “ILC Polarized Electron and Positron Sources” by Kaoru Yokoya (KEK)
- **Polarimetry**
 - “Overview of Electron Polarimetry” by David Gaskell (JLab)
 - “Design of the Beam Polarimeter for FCC-ee” by Nikolai Muchnoi (BINP)
- **Code development and simulations**
 - “Code Development and Simulation Studies of Polarized Beams” by Francois Meot (BNL)
 - “Re-evaluation of Spin-Orbit Dynamics of Polarized e+e- Beams in High Energy Circular Accelerators and Storage Rings: Bloch Equation Approach” by Klaus Heinemann (Univ. of New Mexico)

“Polarized Beams: A Brief History & Future Prospects” by Ya. Derbenev (JLab)

I. Foundations and problems

- Polarization sources
- Thomas – BMT spin equations
- Spin in conventional rings
- Compensated spin rotators
- Resonance depolarization
- Crossing the spin resonances
- ZGS + AGS proton spin acceleration
- BST radiative polarization
- Orlov’ depolarization

II. Polarization canonical theory

III. Siberian Snakes

- SS idea and demonstration
- SS techniques
- SS utilization and success in RHIC
- Multiple SS for SSC

IV. Spin-compensated quads

V. Figure 8 synchrotron

VI. Polarized EIC

- Fixed orbit e-spin rotator and snake

VII. Future polarized beams

- Polarized LHC?
- Polarization ideas for CEPC:

Snakes

Bending snakes

Achromatic snakes

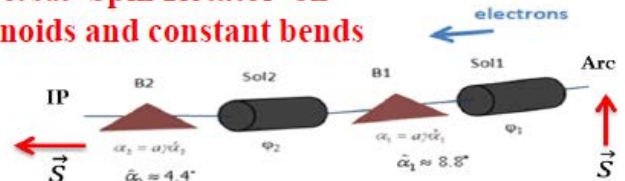
Flipping spin rotators

- Polarization ideas for 75 TeV PPC

Many snakes

Spin-compensated quads

Universal Spin Rotator on solenoids and constant bends



Thoughts on Beam Polarization delivery in CEPC

Option I: Use Polarized e-gun (electrons only...)

- Stacking and accelerating for injection to collider ring
- Acceleration and maintenance of PEB in the Collider Ring

Option II: BST polarization in the Collider Ring

(at injection energy...or in booster ring...?)

- Takes Polarizing Wigglers to facilitate BST
- Luminosity run at wigglers off

Spin Rotators for CEPC.1.

Fixed orbit SR on dipoles and solenoids for CEPC

$$(S_y = 1) \begin{bmatrix} \alpha_{x1} & \alpha_{y1} & \varphi_{z1} & \alpha_{x2} - \alpha_{x1} & \alpha_{y2} & \varphi_{z2} & -\alpha_{x2} \end{bmatrix} (S_z = 1)$$

Spin Rotators for CEPC. 2.

Achromatic Rotator on transverse fields

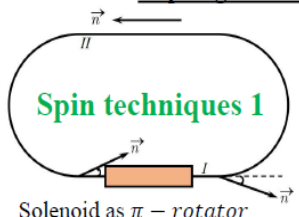
$$(1^{st} \text{ Arc}, S_y = 1) \begin{bmatrix} \alpha_{x1} & \alpha_{y1} & \alpha_{x2} - \alpha_{x1} & \alpha_{y2} & -\alpha_{x2} \end{bmatrix} (IP, S_z = 1)$$

“Siberian Snakes”: making Spin Echo in racetracks...

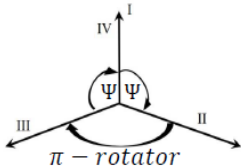
Cancellation idea of spin global precession over the racetrack orbit:
instead of reversing the arcs, let us make *reverse of spin*...!

by inserting local spin flip about a horizontal axis

Topological compensation of spin precession over arcs

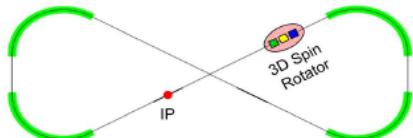


Spin echo effect is obviously extendable to any π -rotator around an arbitrary horizontal axis



Spin Techniques 1

Twisted Spin Synchrotron: Spin Echo



“Polarized Beams: A Brief History and Future Prospects” by Ya. Derbenev

Thinking about Future 75 TeV Polarized Proton Beams. 1.

- Figure 8 Booster in energy range below 30 GeV
- Snakes for the succeeding boosters

Options for the Collider Rings

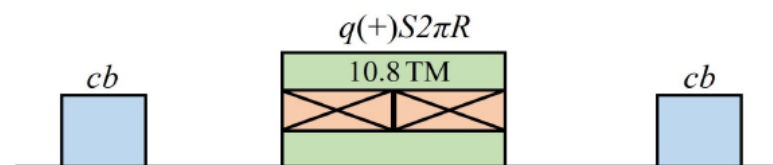
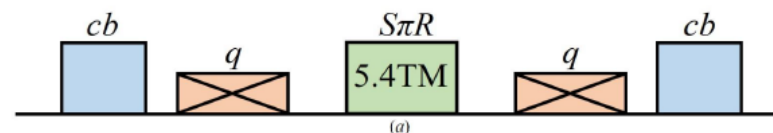
Option I Many SS

- Sufficient large chain of SS to suppress depolarizing impact of the superperiodic misalignment harmonics
- Spin tune $\frac{1}{2}$
- Compensation of tune spread associated with beam emittance
- Spin response function to suppress the beam-beam depolarization

Thinking about Future 75 TeV Polarized Proton Beams. 1.

Thinking about Future 75 TeV Polarized Proton Beams. 2.

Option II: Spin-compensated quadrupoles



- Two SS then will be enough to eliminate spin resonance crossing during the acceleration and stay away of the resonances through the luminosity run
- Think about spin flipping (if inquired); ideas on table..

Preconclusion

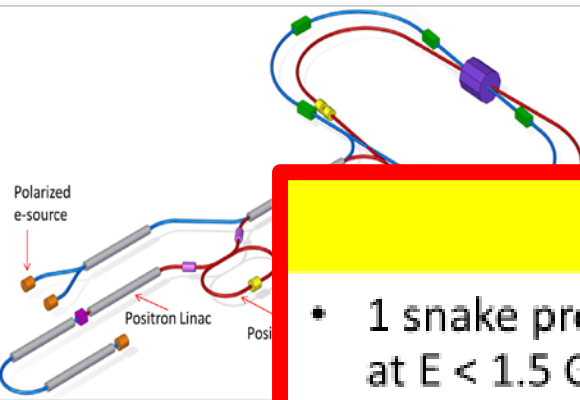
- At this stage, our anticipation of successful design for future polarized beams is close to 100% optimism.

"BINP's Polarization Proposal for Tau-Charm Factory" by I. Koop

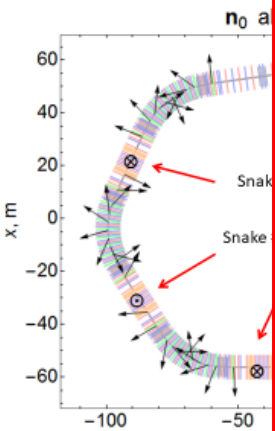
Outline

- BINP's c-tau complex with the longitudinally polarized electrons.

Polarization scheme with 3 snakes (arc=120° +2 damping wigglers in the arc's middle)

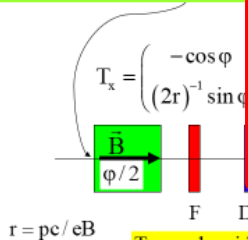


Polarization vector in B



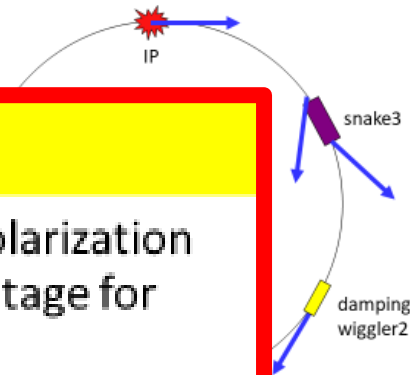
Transparent sp

To decouple x,y-motions



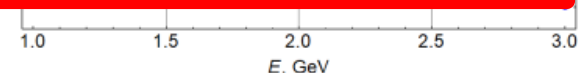
Conclusion

- 1 snake provides up to 80% - 90% of the longitudinal polarization at $E < 1.5$ GeV. This option can be considered as a first stage for polarization program.
- 3 snakes provide sufficiently high polarization degree, about 75-90% in the energy range $E < 2.5$ GeV and only about 50% at 3 GeV. Currently this is the main scenario because it fulfils to the main physics program requirements.
- 5 snakes option requires different optimization of a ring layout to place snakes uniformly in terms of the velocity circulation angle. Now not under consideration.
- Option with two 90° spin rotators is not as universal as multiple snakes version, but its price is much lower. We shall make final choice after discussions with the detector community.



τ_{rad}

- 1 snake
- 3 snakes
- 5 snakes



Two solenoids rotate spin by the total angle ϕ

“Resonant Depolarization at Z and W Beam Energy” by I. Koop

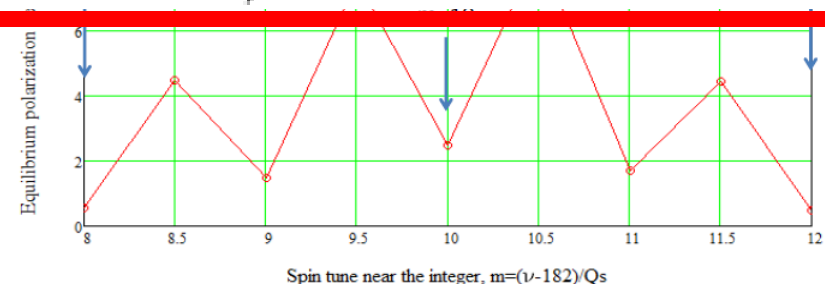
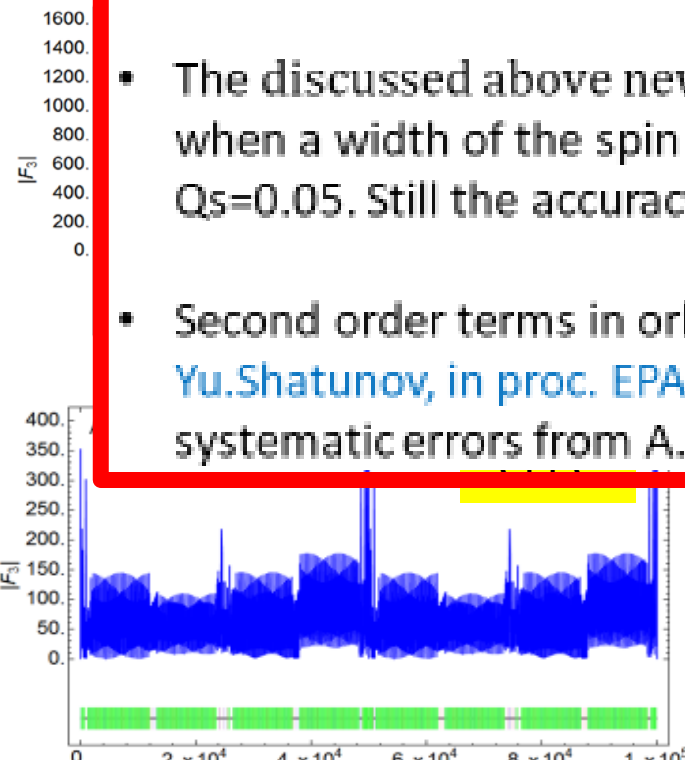
Outline

- Resonance Depolarization studies by spin tracking
- Spin tracking
- Self
- Pro

- Beam emittances in CEPC/FCCee are so small that all resonances with betatron frequencies are suppressed and their influence on the spin motion is negligible

Conclusion

- Spin tracking of a motion of a single particle reveals the dependence of the spectrum line width from the synchrotron tune and other beam parameters.
- This width becomes very large for chosen synchrotron tune $Q_s=0.05$ at W and the standard RD procedure becomes not applicable.
- The discussed above new RD procedure (by steps) works well even in cases when a width of the spin resonance became very large. That is just the case with $Q_s=0.05$. Still the accuracy of a method needs to be studied further.
- Second order terms in orbital motion also contribute to the line width (I.Koop, Yu.Shatunov, in proc. EPAC 1988, Rome, p.738-739). See also the talk on systematic errors from A.Bogomyagkov: tomorrow, WG7.



Polarized electron and positron beams at CEPC by Zhe Duan

Outline

- Motivation
- Prospect and challenges
- Equilibrium beam polarization simulations

Prospects and challenges

- Energy calibration w/ resonant depolarization
- A detailed time diagram of operation with asymmetric wigglers
- Complexities in energy calibration @ W

Motiv

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- tech
- Ho
- “Car
- expe
- new
- Ho
- (?)
- Ar
- W

Discussions

- The simulation results support the theory of uncorrelated regime at ultra-high beam energies, CEPC@120 GeV is expected to be within this regime.
- This study shows there are some open questions to be answered theoretically, Klaus’s talk introduced the status of their investigation, and more progress is expected.

ween
at IPs

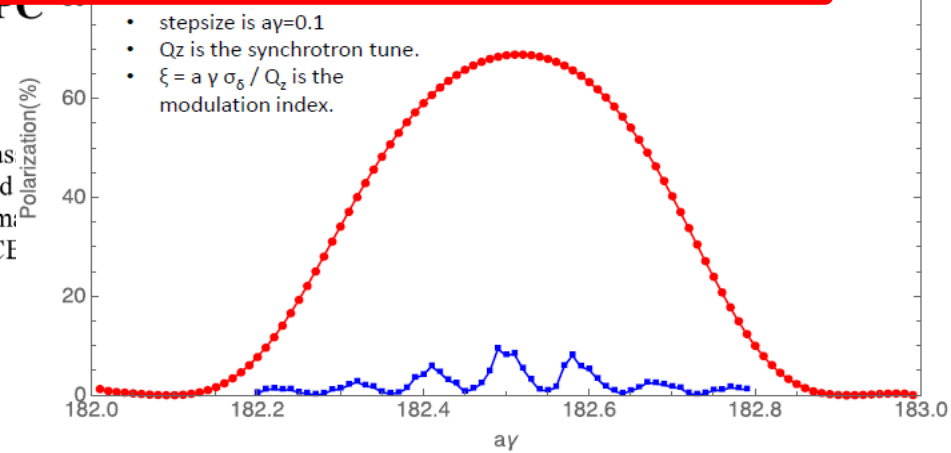
1.87
 $\xi=1.87$

Appendix 8: Opportunities for Polarization in the CEPC

A8.1: Introduction

One of the future experiments at CEPC can be a precise measurement of the mass of the Z using resonant depolarization [1]. To achieve this goal one needs a method of obtaining polarized electron and positron beams. In this appendix we consider the main issues for obtaining the radiative self-polarization of particles with the current CEPC design parameters at 45 GeV and at 80 GeV.

S. Nikitin



- Due to the demanding IR optics design and the machine size, establishing a closed orbit and keeping a stable machine look challenging.
 - Even for an extremely well corrected orbit polarization may reserve surprises, however means have been found for meeting polarization requirements at 45 and 80 GeV beam energy.
- The long τ_p at 45 GeV and short lifetime in collision call for a strategical plan for polarization measurement (see M.Koratzinos IPAC15 contribution):
 - Use of *non-colliding bunches*.
 - Wigglers turned on for the time needed for polarizing the non-colliding bunches while the machine is filled.
 - Exhausted pilote bunches must be immediately replaced (top-up injection needed anyway) so that they get naturally polarized.
- It must be proven that the required calibration precision can be reached. This implies a careful review of all possible biases (see Amsterdam FCC week contributions by A.Bogomyagkov and T.Tydecks):
 - Experiment solenoids, vertical closed orbit and electric fields break the $\nu_s = a\gamma$ relationship.
 - Sawtooth effect.
 - Difference between the energy of non-colliding and colliding bunches.
 - Difference between measured energy and CM energy.
- Energy needs to be monitored routinely.
- Double ring $\rightarrow$ both beams energy needs to be monitored.

- *Resonant de-polarization* ($\ll 100$ keV) at 45 and 80 GeV. It relies on the relationship between the beam energy and the polarization.
- Beam polarization is obtained by the effect of the beam energy because
 - of the build-up rate
 - it is jeopardized by the beam energy which affects the reach
- 10% beam polarization is required for the polarization measurement.

Tools

Accurate simulations are necessary to account for misalignments when direct evaluation of the Derbenev-K expression is prohibitive.

- MAD-X used for simulation of the machine.
- SITROS (by J. Kewish) used for simulation of the beam polarization.
 - Tracking code with 2nd order tracking.
 - Used for HERA-e in the past.
 - It contains SITF (fully 6D) for the spin motion.
 - * Useful tool for preliminary studies.
 - * Computation of polarization is not as useful for disentangling the effects.

More recently Bmad by D. Sagan et al. is available for polarization calculation.

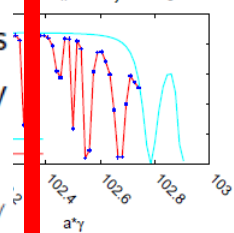
... properly designed with alternating signs.

... Katkov-Strakhovenko

$$\frac{5\sqrt{3}}{8} \frac{r_e \hbar}{m_0 C}$$

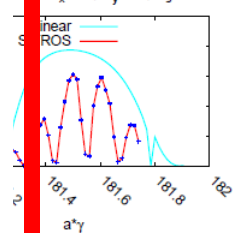
$$c \left[\frac{\hat{B}_w \cdot \hat{n}_0}{|\rho_w|^3} \right]$$

... with $Q_x=0.1, Q_y=0.2, Q_s=0.1$



... monic bumps

... with $Q_x=0.1, Q_y=0.2, Q_s=0.1$



Preliminary Studies of Beam Polarization in CEPC by Wenhao XIA



Outline

- Background
- Questions&Answers about Beam Polarization

(As a beginner)

- 1) What is Polarization?
- 2) Why Polarization?
- 3) How to...?

...

- My Work in the Future
- Summary



Summary

- Polarized electron/positron beams are needed at CEPC to do beam energy calibration and polarization-dependent physics experiments.
- I have learnt some basic theoretical knowledge about beam polarization. For example , Thomas-BMT equation , Sokolov-Ternov effect , Froissart-Stora formula and so on.
- I did some simple calculations with parameters of CEPC. It takes a lot of time to obtain polarization with radiative self-polarization. Special wiggler magnets can speed up this progress.
- My work in the future:
 1. To insert wigglers into the collider ring to speed up radiative self-polarization progress for beam energy calibration .
 2. To overcome/avoid depolarization during acceleration at booster.
 3. To realize the collision of the longitudinally polarized beams at the IPs.

Beam Polarization in Future Colliders: FCC-ee and eRHIC

by Eliana Gianfelice-Wendt

Schematic view of the eRHIC electron accelerators chain

Simulations for the eRHIC storage ring

Summary for eRHIC storage ring

Polarization studies for the eRHIC storage ring are going on.

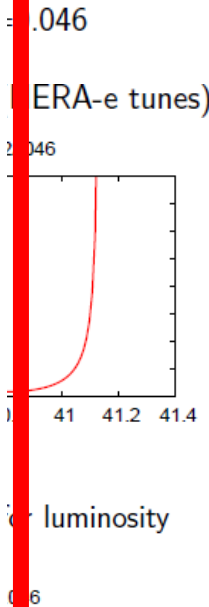
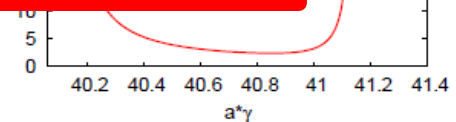
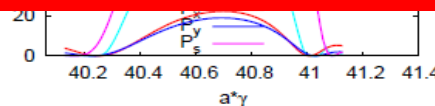
- With conservative errors $P_{\infty} \approx 50\%$ seems within reach:
 - for *upwards* polarized bunches (anti-parallel to the guiding field), $\langle P \rangle \approx 80\%$, over 5 minutes if $P(0)=85\%$;
 - for bunches polarized *downwards* the average polarization drops to 67%: they must be replaced more often.
- Luminosity working point requires linear coupling correction. Here the benefits of a *local correction* using 46 skew quadrupoles have been shown, but
 - the use of correctors for dispersion and of (fewer?) skew quads for betatron coupling correction is an alternative to be tried;
 - implementation of a knob for controlling the vertical beam size at IP w/o affecting polarization seems feasible.
- Comparisons with different codes (Bmad, PTC) are going on.
- Beam-beam effects need to be addressed.

- 494 BPM
- 2x494 cor
- Magnet n
- Optics wi

Assum

hori

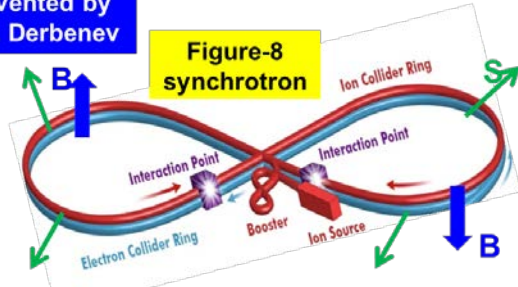
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JLEIC Electron Beam Polarization by Yuhong Zhang

Invented by
Ya. Derbenev

Figure-8
synchrotron

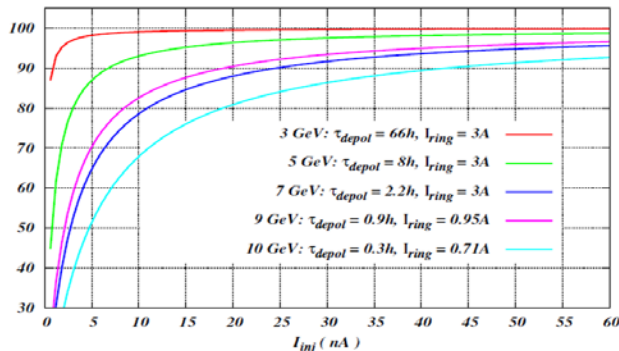


Design concepts

- Figure-8 topology → Enabled by a *green field* collider ring design
- Spin precessions in the left & right parts of a figure-8 ring *exactly cancelled* → spin tune is *zero*
- Does not cross spin resonance during energy ramp
- Spin can be controlled and stabilized by compact spin rotators, no need of Siberian Snakes

Summary

- JLEIC booster and collider rings have adopted a figure-8 shape for better preservation and control of polarization by taking advantage of a spin transparency mode
- Ion and electron polarization schemes have been designed.
- Spin tracking validated figure-8 based polarization control schemes for the whole JLEIC complex
 - Both ion and electron polarizations > 80% can be reached
- Spin transparency mode will be studied in RHIC

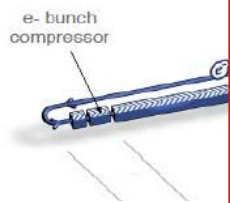


- ~~polarization lifetime same for two spin states~~
- Rotate spin to longitudinal in straights using spin rotators
- **Universal spin rotator**
 - Fixed orbit, energy independent, optics independent

Energy (GeV)	3	5	7	9	12
Lifetime (hours)	116	9	1.7	0.5	0.1

Summary

- Electron source
 - In good shape
 - ~90% polarization can be expected
 - Need some study on the laser
- Positron (undulator)
 - Many issues still remain
 - Water-cooled target → radiation-cooled target
 - FC → QWT
 - Serious design of QWT needed
 - Photon dump
 - Must select undulator or e-driven in early 2021
- Report by Positron WG (May 2018)
 - <http://edmsdirect.desy.de/item/D00000001165115>

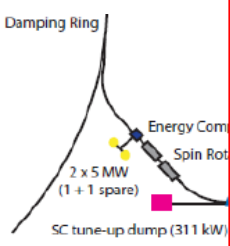


Requirements

- Repetition rate
- Number of bunches per train
- Number of particles per bunch
- Bunch interval
- Rms bunch length

TDR Parameters

- $P > 80\%$
- Photo-cathode
- Drive laser
- Single-bunch



expected

KEK-STF
20nm
seen

is electron

structure
ment afterwards
g the pulse

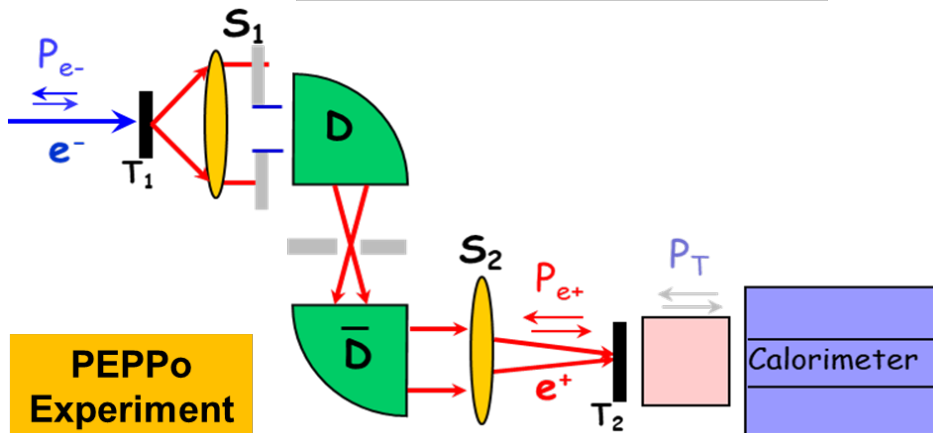
JLEIC Electron Beam Polarization by Yuhong Zhang

Polarized Electrons for Polarized Positrons (PEPPo)

$$\vec{e}^- \rightarrow \gamma \rightarrow \vec{e}^+ (+ \vec{e}^-)$$

E.G. Bessonov, A.A. Mikhailichenko, EPAC (1996)
A.P. Potylitsin, NIM A398 (1997) 395

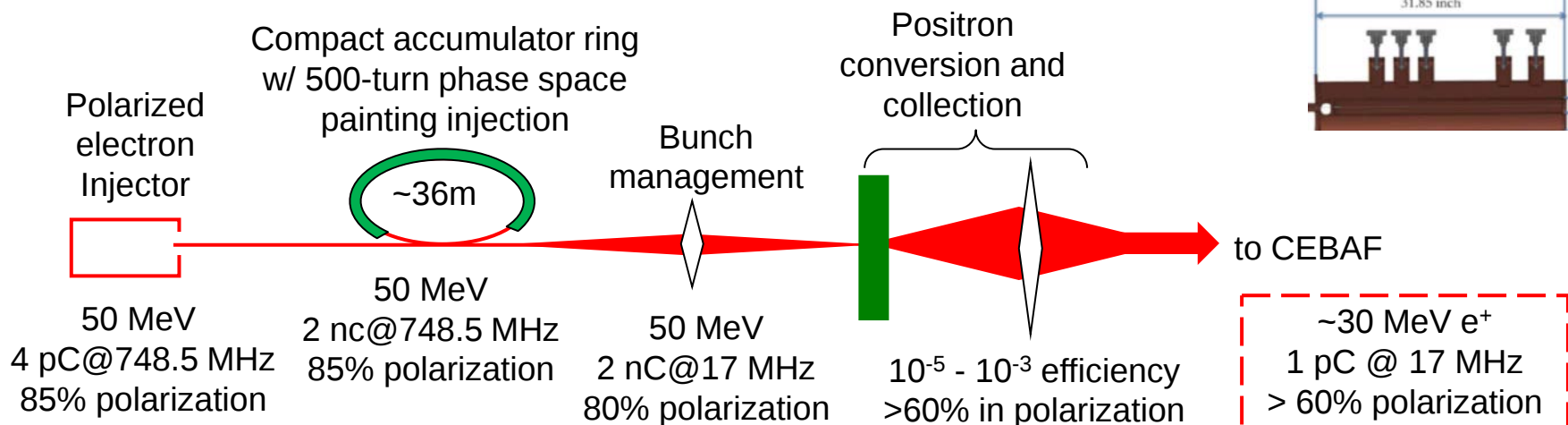
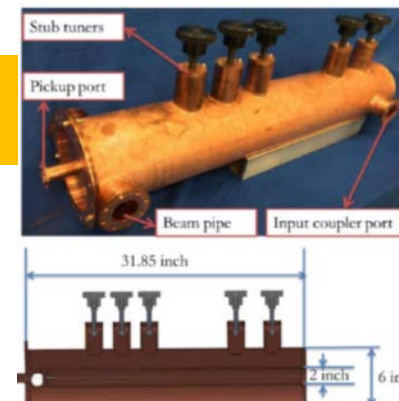
E.A. Kuraev, Y.M. Bystritskiy, M. Shatnev,
E.Tomasi-Gustafsson, PRC 81 (2010) 055208



PEPPo Experiment

- PEPPo provides a new option for polarized positrons in a 10-100 MeV range
 - Pro: low neutron radiation
 - Con: low position yield (10^{-5} to 10^{-3})
- Mitigation of low current: **Accumulation**
 - “hot” positrons after conversion: hard to accumulate with large phase space distribution
 - “cold” electrons before conversion: easy to accumulate

Harmonic RF Kicker



Overview of Electron Polarimetry by Dave Gaskell (JLab)

Outline

- Overview of common electron polarimetry techniques
 - Mott scattering
 - Møller scattering

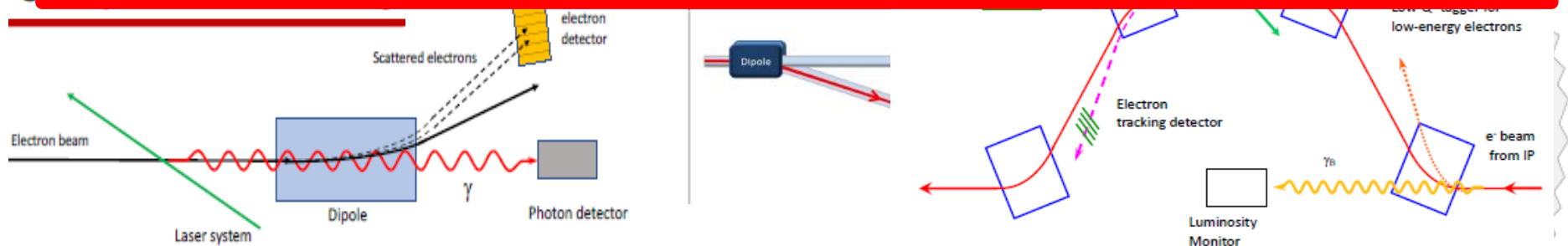
Electron Polarimetry Techniques

Common techniques for measuring electron beam polarization

- Mott scattering: $\vec{e} + Z \rightarrow e$, spin-orbit coupling of electron spin with (large Z) target nucleus
 - Useful at MeV-scale (injector) energies

Summary

- Several useful techniques for electron polarimetry
 - Compton polarimetry is commonly used in storage rings/colliders
 - Møller polarimetry may be possible using jet targets, but likely more R&D is required
- High precision has been achieved with Compton polarimetry with several devices in different accelerators
 - In general, highest precision has used electron detection for longitudinal polarization
 - High precision is possible for transverse Compton polarimeters, but less experience
- EIC will require precise measurements of both electron and hadron polarization
 - Compton polarimeter design for EIC will draw on experience from earlier devices
 - JLEIC (longitudinal) Compton polarimeter design based on successful JLab polarimeters
 - eRHIC Compton polarimeter will measure transverse polarization – important experience from HERA TPOL will prove valuable



Design of the FCC-ee Beam Polarimeter by Nickolai Muchnoi

Excerpts from FCC-ee CDR

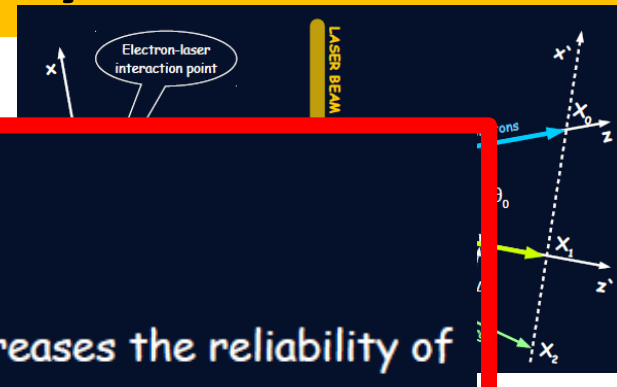
- ▶ Beam energy precise ~ 100 keV
- ▶ About 2 frequencies
- ▶ It is important energy asymptotically
- ▶ E_{cm} near reconstruction of the

Summary

- ▶ Detecting both scattered photons & electrons increases the reliability of beam polarization measurement.
- ▶ FCC-ee polarimeter provides $\simeq 1\%$ / s accuracy for $\zeta_{\perp}$.
- ▶ The beam energy spectrometer option does not require mandatory neither the B-field measurement nor the BPMs data:
 - ▶ statistical precision $\Delta E/E \simeq 100$ ppm / 10 sec;
 - ▶ systematic effects estimation requires further studies: yet no limitations;
 - ▶ test of the approach does not require high beam energy and should be performed with low emittance beam at low energy.
- ▶ Polarimeter allows to measure beam sizes & positions.

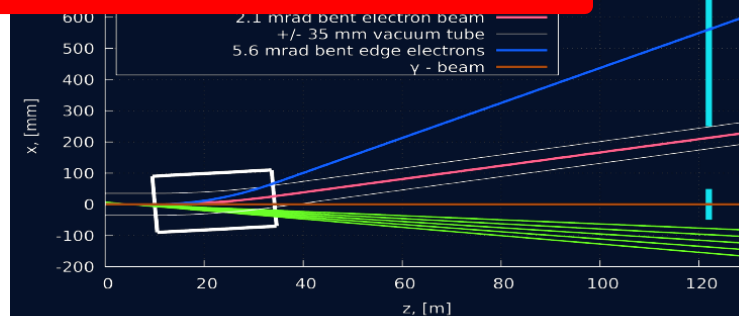
Polar

- ▶ Fast measurement energy
- ▶ Positive
- ▶ Known polarization
- ▶ Inverse Compton scattering is used for direct beam energy calibration at low-energy $e^{\pm}$ colliders: VEPP-4M, BEPC-II, VEPP-2000.
- ▶ Extend the latter experience for high energy colliders?



straight section

2.33 eV, $\kappa = 1.63$.



Blue bars - 2D silicon pixel detectors for scattered electrons & photons.

Code Development and Polarized Beam Simulation Studies

by Francois Meot (BNL)

Contents

- 1 ZGOUBI
- 2 Hadron polarization at RHIC complex
- 3 Electron polarization in eRHIC
- 4 Hadron polarization in eRHIC
- 5 JLEIC EIC
- 6 Cornell-BNL CBETA FFAG ERL

Numerical integrator

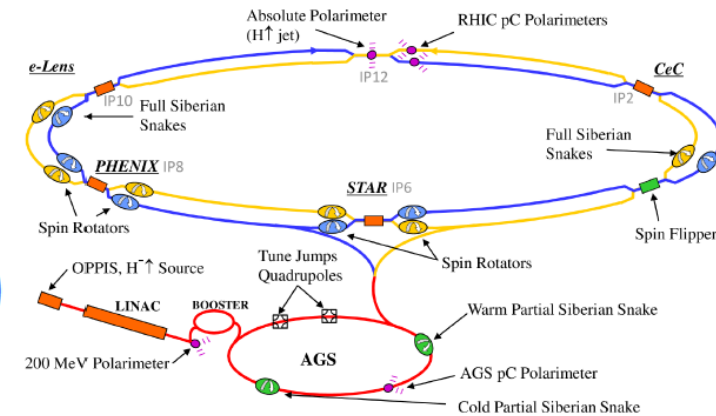
$$\frac{d(\mathbf{m}\tilde{\mathbf{v}})}{dt} = q\tilde{\mathbf{v}} \times \tilde{\mathbf{b}}$$

$$\frac{d\tilde{\mathbf{S}}}{dt} = \frac{q}{m}\tilde{\mathbf{S}} \times \tilde{\omega}$$

$$(\tilde{\omega} = (1 + \gamma G)\tilde{\mathbf{b}} + G(1 - \gamma)\tilde{\mathbf{b}}_{//})$$

◇ Zgoubi was first written in 1972... 45⁺ yrs !

◇ Installed in sourceforge in 2007



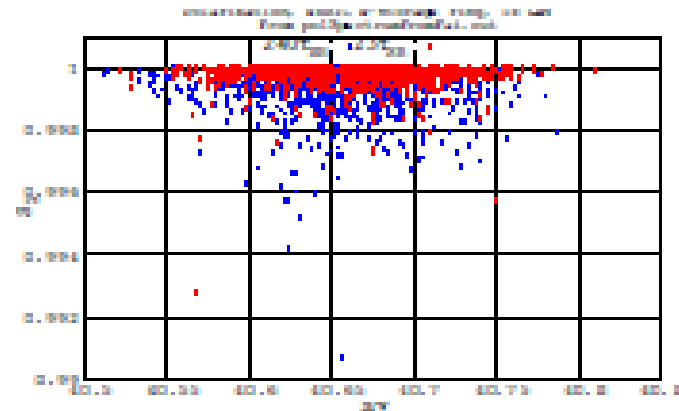
2 Hadron polarization at RHIC complex

- include p, He3
- start at the booster, and include AGS, AtR, RHIC

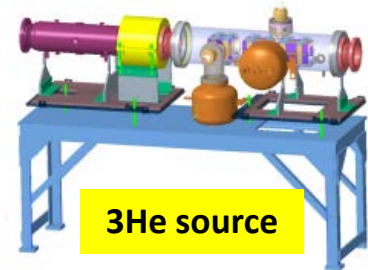
Electron polarization in eRHIC

Polarization lifetime in eRHIC storage ring

- Spins tracked over 240 damping times in eRHIC, 18 GeV



support the eRHIC polarized ³He project



3He source

Spin Tracking Helium-3 through 12-

From Run14: normalized 95% emittance, $\varepsilon_N = 4.78$ mm mrad measured at MW006.
 $\varepsilon_N = 5.0$ mm mrad used for the simulations, $\sigma_y = 2.65$ mm.
 $\alpha = 2.654 \times 10^{-6}$

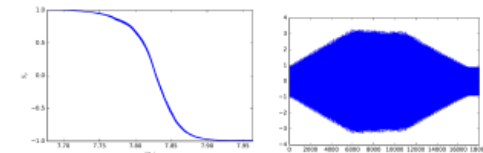
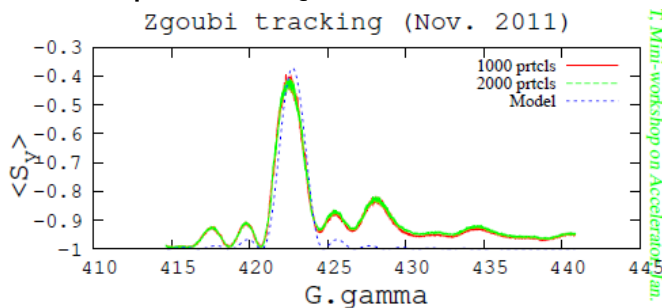


Figure 1: Spin tracking results for Helium-3.

Booster simulations

- Used over past 10 yrs to study polarization in RHIC.
- A benchmarking example: crossing the strong snake resonance $G\gamma = 393 + Q$



T. Mini-workshop on Acceleration

Re-evaluation of Spin-Orbit Dynamics of Polarized e⁺e⁻ Beams in High Energy Circular Accelerators and Storage Rings: Bloch equation approach by Klaus Heinemann (Univ. New Mexico)

Outline

- Topic: Is polarization possible in high energy electron storage rings like proposed Circular Electron Positron Collider (CEPC) and Future Circular Collider (FCC-ee)?
- Review standard approach: Derbenev-Kondratenko formulas
- Derbenev-Kondratenko formulas rely, in part, on plausible assumptions grounded in deep physical intuition²
- Question: Do Derbenev-Kondratenko formulas, even with correction terms, tell full story?
- Alternative approach: Bloch equation for polarization density³
- Bloch equation allows for assessment of Derbenev-Kondratenko formulas
- Numerical approach to Bloch equation suggests Method of Averaging for getting effective Bloch equation
- Hope: Bloch equation teaches us domain of applicability of Derbenev-Kondratenko formulas

Derbenev-Kondratenko-formula

$$P_{DK}(\theta) = P_{DK}(+\infty)(1 - e^{-\theta/\tau_{DK}}) + P_{DK}(0)e^{-\theta/\tau_{DK}}$$

$$P_{DK}(+\infty) = \frac{\tau_0^{-1}}{\tau_{DK}^{-1}}$$

$$\tau_{DK}^{-1} = \frac{5\sqrt{3}}{8} \frac{r_e \gamma^5 \hbar}{m} \frac{C}{4\pi^2} \int_0^{2\pi} d\theta \frac{1}{|\rho(\theta)|^3} \left\langle 1 - \frac{2}{9} (\vec{n} \cdot \hat{\beta})^2 + \frac{11}{18} \left| \frac{\partial \vec{n}}{\partial z_6} \right|^2 \right\rangle$$

$$\textcircled{1} \tau_0^{-1} = \frac{r_e \gamma^5 \hbar}{m} \frac{C}{4\pi^2} \int_0^{2\pi} d\theta \frac{1}{|\rho(\theta)|^3} \left\langle \hat{b} \cdot \left[\vec{n} - \frac{\partial \vec{n}}{\partial z_6} \right] \right\rangle_\theta$$

- ① Fokker-Planck equation for phase space density:

$$\partial_t f_{lab} = \underbrace{L_{lab}(t, r, p) f_{lab}}_{\text{Liouville \& damping \& diffusion}} \quad (1)$$

- ② Bloch equation for polarization density:

$$\begin{aligned} \partial_t \vec{\eta}_{lab} = & \underbrace{L_{lab}(t, r, p) \vec{\eta}_{lab}}_{\text{Liouville \& damping \& diffusion}} + \underbrace{\vec{\Omega}_{lab}(t, r, p) \times \vec{\eta}_{lab}}_{\text{T-BMT-terms}} \\ & + \underbrace{G_{lab}(t, r, p) \vec{\eta}_{lab} + \vec{g}_{lab}(t, r, p) f_{lab}}_{\text{spin-flip terms}} \end{aligned} \quad (2)$$

- Description of electron bunch by spin-1/2 Wigner function ρ_{lab} :

$$\rho_{lab}(t, r, p) = \frac{1}{2} [f_{lab}(t, r, p) I_{2 \times 2} + \vec{\sigma} \cdot \vec{\eta}_{lab}(t, r, p)]$$

- Bloch equation is PDE describing linear driven oscillator with damping and diffusion
- Task: Find equilibrium polarization vector $\vec{P}_{lab}(\infty)$
- Bloch equation generalizes Baier-Katkov-Strakhovenko ODE to include phase-space effects⁸

Future work

- Further development of Bloch equation approach (numerical and theoretical)
- Comparing the Bloch equation approach with Derbenev-Kondratenko-formula approach
- Better understanding/modification of Derbenev-Kondratenko-formula approach
 - ① Study of correction term to τ_{DK}^{-1} in terms of RBE
 - ② Replacing the invariant spin field $\vec{n}$ by “radiative invariant spin field”
 $\vec{p} \Rightarrow \left| \frac{\partial \vec{n}}{\partial z_6} \right|^2$ replaced by $\left| \frac{\partial \vec{p}}{\partial z_6} \right|^2$ ²⁰

Personal Impression and Prospect

- There is a theoretical framework of beam polarization and good understanding
- There were successful experiences in dealing beam polarizations in collider
 - Lepton beam polarization in HERA
 - Hadron beam polarization in RHIC
- Very challenging beam polarization requirements in future colliders
 - $\sim 10\%$ polarization for both e^- and e^+ beams in z (and even W) energy
 - $>70\%$ polarization for both electron and proton/light ion beams in EIC
- More challenges in delivering physics: spin flip
- Technical systems: polarized sources (ILAC, Super Tau-Charm, EIC)
- Technical system: polarimetry
- There are good simulation tools, still need improvements (physics and computing)
- A small community, international collaboration should be very helpful